

Linear - Quiz 2

Name: _____

1. (4 points) Let $\mathbf{u} = \begin{bmatrix} 3 \\ -2 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$. Show that $\begin{bmatrix} a \\ b \end{bmatrix}$ is in $\text{Span}\{\mathbf{u}, \mathbf{v}\}$ for all a and b .

2. (2 points) Construct a 4×4 matrix, not in echelon form, whose columns span \mathbb{R}^4 . Show that the matrix you construct has the desired property. Hint: Keep it simple, but not in echelon form.

3. (4 points) Let $v_1 = \begin{bmatrix} 1 \\ 0 \\ -1 \\ 0 \end{bmatrix}$, $v_2 = \begin{bmatrix} 0 \\ -1 \\ 0 \\ 1 \end{bmatrix}$ and $v_3 = \begin{bmatrix} 1 \\ 0 \\ 0 \\ -1 \end{bmatrix}$. Does $\{v_1, v_2, v_3\}$ span \mathbb{R}^4 ? Why or why not?