

Business Calculus, MiniTest 1 Review

Dr. Graham-Squire, Fall 2014

•The test will cover sections 1.1 through 2.3.

•To study, you should look over your notes, rework HW problems on WebAssign, quizzes, and problems from the notes, as well as work out the practice problems given for each section. The Review Questions at the end of Chapters 1 and 2 are also good practice (in the Chapter 2 review you should skip all questions involving derivatives and limits, since that is not covered on this test).

•You can also look at Minitest 1 from Fall 2012 on my website, as well as Test 1 from Summer 2012, though you must be careful- not all of those questions from Test 1 (Summer) will show up on this test because that test covered up through section 2.5. In particular, you can ignore any question that involves “limits” (numbers 4, 5, and most of 6. You should be able to sketch the graph for number 6). Also, Question 5 from Test 2 (from Fall 2012) is another type of question that could show up on this test.

•Calculators are allowed on this test, but for certain questions you may not be allowed to use a calculator. It is highly recommended that you bring a calculator because you cannot use cell phones or computers during the test.

•Some practice problems to work on:

1. Factor and simplify the expression $5x^2(3x^2 + 1)^4(6x) + (3x^2 + 1)^5(2x)$.

2. The average speed of a vehicle in miles per hour over a certain stretch of road, between 6 AM and 8 AM, is given by

$$20t^2 - 40t + 50 \quad (0 \leq t \leq 2)$$

where t is in hours, with $t = 0$ corresponding to 6 AM. Over what interval(s) of time is the average speed less than or equal to 35 mph?

3. Dominic has decided to attach his baby sister Eva to a rocket. Suppose Dominic is standing 200ft from the rocket (over flat ground) and the rocket with Eva attached lifts off vertically in the air and reaches an altitude of x feet.

(a) Find an expression (in terms of x) giving the distance between Dominic and Eva as the rocket goes up.

(b) What is the distance between Dominic and Eva when the rocket reaches an altitude of 1,000 feet? Round to the nearest whole number.

4. Find the equation of the line that passes through the points (1,2) and (-3,-2), and write the equation in the form $y = \underline{\hspace{2cm}}$. Is the point (4, 8) also on that line? Explain why or why not.

5. Sketch the graph of the function $f(x) = \begin{cases} 4 - x & \text{if } x < 2 \\ 2x - 2 & \text{if } x \geq 2 \end{cases}$

6. Find the rules for the composite functions $f(g(x))$ and $g(f(x))$ if $f(x) = \frac{x}{x^2 + 5}$ and $g(x) = \frac{1}{x^2}$. Simplify the resulting expressions.

7. The sales of DVD players in year t (in millions of units) is given by the function

$$f(t) = 5.6(1 + t) \quad (0 \leq t \leq 3)$$

where $t = 0$ corresponds to 2001. Over the same period, the sales of VCRs (in millions of units) is given by

$$g(t) = \begin{cases} -9.6t + 22.5 & \text{if } 0 \leq t \leq 1 \\ -0.5t + 13.4 & \text{if } 1 < t \leq 2 \\ -7.8t + 28 & \text{if } 2 < t \leq 3 \end{cases}$$

- (a) Show that more VCRs than DVD players were sold in 2001.
(b) When did sales of DVD players first exceed those of VCRs?
8. Farmer Bob wants to enclose a rectangular area next to his barn with fencing. One side of the rectangular area will be the side of the barn, and the other three sides will be fencing. Suppose that Bob has 80 feet of fencing and his barn is 100 feet long.
- (a) If the width of the rectangular area is x , find an expression for the area of the rectangle.
(b) If the width is 10 feet, what will the area of the rectangle be?